

## Algebra.

## 1. Equalities: equations and identities

## Inequalities.

We can add any number to both part of the inequality, the sign ( $\langle$ or $>$ ) will not change:
$x>-1$

| -4 | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 1 |  | 1 | 0 | 1 | 2 | 3 |
| -4 | -3 | -2 | -1 | 0 | 4 |  |  |  |

$x+2>-1+2 \Rightarrow x+2>1$
$y-3<5$
$y-3+3<5+3$


1. $x+3>-5$

Now let's try to multiply or divide both part of the inequality by the positive number.
 If $x>3$, then $2 x$ will be grater then 6 .
$x>3, \quad 2 x>6$

If $x>3$ what can we tell about $-x$ ?
$-x \quad 3 \cdot(-1)$
2. $x+3>5 x-5$
3. $4 \mathrm{x}-3 \neq 0$
4. $3(x-1)<5 x+9$
5. $2 x-1>-x+3$
6. $|x|>8$
7. Show on the number line points that are satisfying the following inequalities:
a) $|x|<4$

| 9 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | -8 | -7 | -6 | -5 | -4 | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |

b) $|x|>3$

| -9 | -8 | -7 | -6 | -5 | -4 | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

c) $\left|x-\frac{1}{2}\right|>3$

| 9 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -9 | -8 | -7 | -6 | -5 | -4 | -3 | -2 | -1 | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |

d) $\left|x-\frac{1}{2}\right|<8$

8. $M=\{x \mid x>5\}, K=\{x \mid x<20\}$
$M \cap K=$
$M \cup K=$
9. $\quad M=\{x \mid x \leq 5\}, K=\{x \mid x \geq 20\}$
$M \cap K=$
$M \cup K=$
10. Points $a, 0$, and $b$ are marked on the number line below:


Which of the following expressions is true?

1) $a+b>0$ or $a+b<0$
2) $a b>0$ or $a b<0$
3) $a-b>0$
or $a-b<0$
4) $\frac{b}{a}>1$ or $\frac{b}{a}<1$
11. Points $a, b, c, 0$, and 1 are marked on the number line below:


Which of the following expressions is true?

1) $a b<b$ or $a b>b$
2) $a b c<a$ or $a b c>a$
3) $-a c<c$ or $-a c>c$
12. Sum of the internal angels of any polygon is $(n-2) \times 180$.

$$
n \times 180-360=(n-2) \times 180
$$


13. Compute the area of the figures below. The picture is not to scale, so do not try measuring the lengths - use the numbers given. In the last one, the area of the shade d part.


5


