

## Math 4a. Homework 11.

Problems marked with \* are more difficult.



1. Solve the following equations:

a)  $\left|x + \frac{1}{2}\right| = 3$

b)  $\left|x - \frac{1}{2}\right| = 3$

c)  $|2y| = 5$

d)  $|2z + 2| = 6$

2. A cook put 3 tablespoons of salt into a pot with 4 liters of water and 2 tablespoons of salt into a pot with 3 liters of water. Which pot has saltier water?

3. There are three people (Alex, Brook and Robert), one of whom is a knight, one is a knave, and one is a spy.



The knight always tells the truth, the knave always lies, and the spy can either lie or tell the truth.

Alex says: "Robert is a knave."

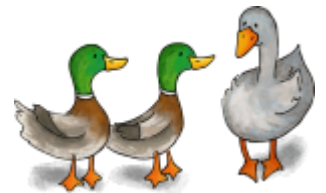
Brook says: "Alex is a knight."

Robert says: "I am the spy."



Who is the knight, who is the knave, and who is the spy?

4. \* 4 little ducklings and 5 little geese weight 4 kg and 100 g. 5 little ducklings and 4 little geese weight 4 kg. How much does one little goose weight?



5. Fill the empty spaces in the table:

$a$	$b$	$a - b$	$b - a$
20	7		
-15	8		
30	-9		
-10	-6		

6. Compute:

$$\text{a) } \frac{2 - \frac{1}{\frac{1}{2} + \frac{1}{4}}}{2 + \frac{1}{\frac{1}{2} + \frac{1}{4}}};$$

$$\text{c) } 1 - \frac{1}{1 + \frac{1}{2}};$$

$$\text{e) } 1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{2}}};$$

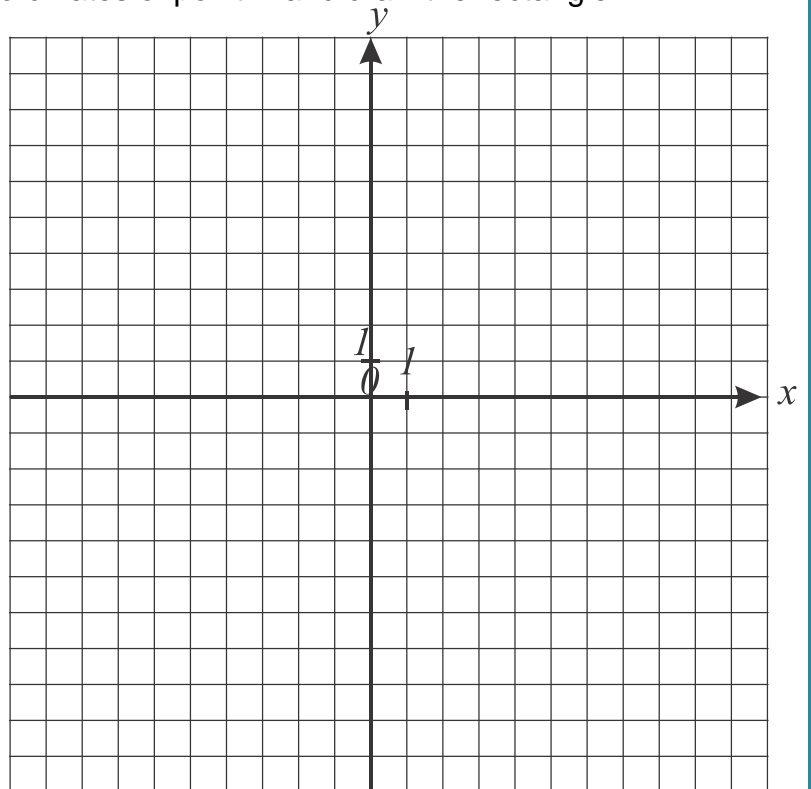
$$\text{b) } \frac{4 + \frac{1}{\frac{1}{2} - \frac{1}{3}}}{4 - \frac{1}{\frac{1}{2} - \frac{1}{3}}};$$

$$\text{d) } 2 + \frac{2}{1 - \frac{2}{3}};$$

$$\text{f) } 3 - \frac{3}{3 - \frac{1}{1 - \frac{1}{3}}}.$$

7. ABCD is a rectangle. Find the coordinates of point D and draw the rectangle.

- a. A(-9; 2), B(-9; 4), C(-3; 4)
- b. A(0; 6), B(0; -2), C(5; -2)
- c. A(9; 0), B(9; -5), C(2; -5)
- d. A(-6; 0), B(-6; -7), C(0; -7)



8. There are singers and dancers in our class.  $\frac{1}{5}$  of all singers also dance and  $\frac{1}{4}$  of all dancers also sing. Are there more singers or dancers in our class?