

## Homework 15

### Electric potential

The potential energy where of two charges separated by a distance  $r$  is

$$P = k \frac{q_1 \cdot q_2}{r} \quad (1)$$

Let us keep one of the charges, say,  $q_1$  fixed and change the charge  $q_2$ . Since there is a product of the charge magnitudes in the numerator of formula (1), the potential energy will increase or decrease together with the charge magnitude of  $q_2$ . We can now calculate the potential energy *per unit charge*. For this we will divide the potential energy of the interacting charges  $q_1$  and  $q_2$  by the magnitude of  $q_2$ :

$$\frac{P}{q_2} = k \frac{q_1 \cdot q_2}{r} \div q_2 = k \frac{q_1}{r} \quad (2)$$

We can imagine that each point of space around the charge  $q_1$  can be characterized by the potential energy of a positive unit charge in this point. The electrostatic potential energy of a positive unit charge in a certain point is called “*electric potential*” in this point. The electric potential is a scalar.

The electric potential  $\varphi$  created by the point charge  $q$  is:

$$\varphi = k \frac{q}{r} \quad (3)$$

*If the charge  $q$  is negative, the potential will be negative as well.*

The formula (3) means that a unit positive point charge placed at the distance  $r$  from the charge  $q$  will have potential energy  $\varphi$ . If we will place an arbitrary charge  $Q$  at the distance  $r$  (instead of a unit charge) then the potential energy of the charge  $Q$  can be calculated as:

$$P = k \frac{q}{r} \cdot Q = \varphi \cdot Q \quad (4)$$

As we can see from the formula (3) the potential created by a point charge depends on the distance to the point charge. Difference of potentials taken in points A and B equals to the difference of potential energy of a unit positive charge in these points. As (I hope) you remember difference of potential energy of an object in points B and A is also equal to the work  $W_{AB}$  of the electric force to transfer the unit positive charge from point A to point B. If a charged object with a charge  $q$  moves from point A to point B, the work of the electric force is:

$$W_{AB} = P_A - P_B = q\varphi_A - q\varphi_B = q(\varphi_A - \varphi_B) = qU_{AB}$$

Here  $P_A, P_B$  –electrostatic potential energies in points A and B;  $\varphi_A, \varphi_B$  – the electrostatic potentials,  $U_{AB} = \varphi_A - \varphi_B$  is the potential difference which is also called “*voltage between points A and B*”.

Problems:

1. An object with a charge of  $0.01\text{C}$  being accelerated by electrostatic force moves from point A to point B and gains kinetic energy of  $6\text{J}$ . Find the potential difference between points A and B.
2. There is a point charge of  $-1\text{C}$  (see picture below). The distance between the charge and the point A is  $100\text{m}$ , the distance between the points A and B is also  $100\text{m}$ . Find the potential difference between points A and B.

