## The Metric System



Customary and international system (SI) units

kilometer centimeter


## The International System of Units

## Origin of the Metric System

- Idea of standardized system of measurement based on the decimal was first proposed as early as $\sim 1670$.
- The first practical implementation was carried out by French Revolutionaries towards the end of the 18th century.
- In 1790 a committee (including mathematicians Laplace and Legendre, and chemist Lavoisier) was appointed to develop a unified, natural, universal system of measurement.


It was called the "metric" system (French for measure).

## Metric System Basics

- The metric system was built around three base units that corresponded to a certain kind of measurement:
$>$ Length = meter
$>$ Volume = liter
$>$ Weight (Mass) = gram
- The base units were derived from the natural world: the dimensions of the Earth and properties of water.
- Decimal multiplicative prefixes were added to base units to make up the full range of metric system:
> Milli + meter $=$ millimeter
$>$ Kilo + gram $=$ Kilogram
- Historically, prototypes ("originals") of base units were kept in the Archives Nationales in France with copies manufactured and distributed among other 17 countries - members of The Metre Convention of 1875.


## Fundamental Units

By design, the base units used in the Metric System must be realizable, ideally with reference to natural phenomena.

As Metric System evolved into the SI system, seven mutually independent fundamental units have been selected:

1. Meter (length)
2. Kilogram (mass)
3. Second (time)
4. Kelvin (temperature)
5. Ampere (electric current)
6. Candela (luminous intensity)
7. Mole (amount of elementary
 entities like atoms or molecules)

## The Meter, m (Metric, SI)

- Original definition (1791): one ten millionth $(1 / 10,000,000)$ of the quarter of the Earth's meridian (distance between the North Pole and the Equator through Paris was determined based on a Pierre Méchain and Jean-Baptiste Delambre 1792-1798 survey of the length of the Earth's meridian between Dunkirk ( $51^{\circ} \mathrm{N}$ ) and Barcelona ( $41^{\circ} \mathrm{N}$ ) through Paris).
- 1799: platinum bar, known as the mètre des Archives. The International Metre Commission in Paris (1870-72, 1875): new "metric prototypes" made of $90 \%$ platinum and $10 \%$ iridium.
- 1983: One meter is the distance traveled by a ray of light through a vacuum in $1 / 299,792,458$ second. The definition in terms of the speed of light means that the meter can be realized using any light source of known frequency, rather than defining a "preferred" source.



## The Liter, L (Metric, non-SI)

- Unit of volume, one of three original base units in metric system circa 1799.
- Volume = Length $\times$ Width $\times$ Height
- The liter is equal to 1 cubic decimeter ( $10 \times 10 \times 10$ centimeters) or $1 / 1,000$ cubic meter.
- One liter of liquid water has a mass of almost exactly one kilogram.
- Most commonly used for fluids and solids that can be poured (which are measured by the capacity or size of their container).


## The Gram and the Kilogram, g and kg (Metric, si )

- Mass: the amount of matter in an object.
- The gram, 1795: the mass of one cubic centimeter of water at the melting point of water.
- The original prototype kilogram manufactured in 1799 had a mass equal to the mass of 1.000025 liters of water at $4^{\circ} \mathrm{C}$.
- 1875: The International Prototype Kilogram, a cylinder of platinum/platinum-iridium alloy.
- Kilogram is the only SI unit that is still directly defined by an artifact.
- 2005: International Committee for Weights and Measures recommended that the kilogram be redefined in terms of a fundamental constant of nature.




## The Second, s (Metric, SI)

- Earliest documented scientific use of second as a unit of time: $\sim 1000$ by Persian scholar al-Biruni.

- Carl Friedrich Gauss, 1832: proposed to use second as a base unit.
- Original definition: 1/86,400 of a mean solar day (the Earth's rotation is slowing down, so in this definition a second was not a constant...)
- International Astronomical Union, 1952-1956 redefinition: the fraction $1 / 31,556,925.9747$ of the tropical year 1900.
- Current definition (developed by General Conference on Weights and Measures in 1967 and refined in 1997): definition using atomic clocks as the duration of $9,192,631,770$ periods of the radiation corresponding to the transition between the two hyperfine levels of the ground state of the caesium-133 atom at rest at a temperature of 0 K .

- SI prefixes starting from millisecond are commonly used to measure time less than a second (submultiples); non-SI units minutes, hours, days, Julian years, Julian centuries, and Julian millennia are used to measure multiples of second.


## The Kelvin, K (SI)

- Unit of thermodynamic temperature (absolute temperature).
- Original (1743): the centigrade scale (renamed "Celsius" in 1948) is obtained by assigning $0^{\circ} \mathrm{C}$ to the freezing point of water and $100^{\circ} \mathrm{C}$ to the boiling point of water both at a pressure of one standard atmosphere with mercury being the working material.

- Current (1967): 1/273.16 of the thermodynamic temperature of the triple point of water (triple point of water $=273.16 \mathrm{~K}=0.01^{\circ} \mathrm{C}$ by definition).


## Prefixes in Metric System

| Prefix | Symbol | Factor |  |
| :---: | :---: | :---: | :---: |
| tera | T | 1000000000000 | $10^{12}$ |
| giga | G | 1000000000 | $10^{9}$ |
| mega | M | 1000000 | $10^{6}$ |
| kilo | k | 1000 | $10^{3}$ |
| hecto | h | 100 | $10^{2}$ |
| deca | da | 10 | $10^{1}$ |
| (none) | (none) | 1 | $10^{\circ}$ |
| deci | d | 0.1 | $10^{-1}$ |
| centi | c | 0.01 | $10^{-2}$ |
| milli | m | 0.001 | $10^{-3}$ |
| micro | $\mu$ | 0.000001 | $10^{-6}$ |
| nano | n | 0.000000001 | $10^{-9}$ |
| pico | p | 0.000000000001 | $10^{-12}$ |

## Scientific Notation

- Scientific notation (also referred to as "standard form" or "standard index form") is a way of writing numbers that are too big or too small to be conveniently written in decimal form.
decimal point
$6.02 \times 10^{23}$
a real number with an absolute value
between 1 and 10
an order of magnitude value written as a power of 10
- When using SI system, order of magnitude is restricted to follow standard SI prefixes; the resulting number representation is called "engineering notation".


## What is the order of the metric system?

- King Henry Died by Drinking Chocolate Milk larger
- King: Kilo
- Henry: Hecto
- Died: Deca
- By: Base (m, L, g)
- Drinking: Deci
- Chocolate: Centi
- Milk: Milli



## Examples

Any US paper currency note (\$1, \$5, \$10, \$20) has a mass of 1 g ; the mass of a nickel is 5 g ; the mass of a penny is $\mathbf{2 . 5}$ grams.


A typical doorknob is $\sim 1 \mathrm{~m}$ high.


The mass of the Earth is $6 \times 10^{24} \mathrm{~kg}$; the mass of the Moon is $7.3 \times 10^{22} \mathrm{~kg}$; the mass of the Sun is $1.99 \times 10^{30} \mathrm{~kg}$.

Typical airport runway length is 3.35 km; Boeing 767 jet is 64 m long.


Diameter of Influenza virus is $\mathbf{\sim} \mathbf{2 0 ~} \mathrm{nm}$.

The diameter of a CD or a DVD is 12 cm ; the diameter of the center hole is 15 mm .

## Imperial-Metric Equivalences

- Units of Weight
$-1 \mathrm{oz}=28.35 \mathrm{~g}$
$-1 \mathrm{lb}=454 \mathrm{~g}$
$-2.2 \mathrm{lb}=1 \mathrm{~kg}$
- Units of Capacity
-1.06 qt $=1 \mathrm{~L}$
$-1 \mathrm{gal}=3.79 \mathrm{~L}$
- Units of Length
$-1 \mathrm{in}=2.54 \mathrm{~cm}$
$-3.28 \mathrm{ft}=1 \mathrm{~m}$
- $1.09 \mathrm{yd}=1 \mathrm{~m}$
$-1 \mathrm{mi}=1.61 \mathrm{~km}$


