## MATH 10

## ASSIGNMENT 23: TRIANGULATIONS

MAY 8, 2022

## Homework

1. Prove that the connected sum of two surfaces is a surface and that, for any surface $S$, the connected sum of $S$ with the sphere is homeomorphic to $S$.
2. What surface is obtained if one shrinks the boundary circle of a Möbius strip to a point?
3. Find a triangulation of the projective plane.
4. Which of these are triangulated surfaces?
(a) $\mathrm{ABD}, \mathrm{BCD}, \mathrm{ACD}, \mathrm{ABE}, \mathrm{BCE}, \mathrm{ACE}$
(b) ABE,BCE,CDE,ABF, $\mathrm{BCF}, \mathrm{ADF}, \mathrm{AEF}, \mathrm{ADE}$
(c) $\mathrm{ABC}, \mathrm{BCD}, \mathrm{CDE}, \mathrm{ADE}, \mathrm{ABE}, \mathrm{CEF}, \mathrm{BEF}, \mathrm{BDF}, \mathrm{ADF}, \mathrm{ACF}$
