## Math 2 Classwork 19

## Warm Up

A square was composed of 25 small squares, but some of these small squares are lost. How many are lost?

(A) 6
(B) 7
(C) 8
(D) 10
(E) 12

2 The kangaroo is inside how many circles?
(A) 1
(B) 2
(C) 3
(D) 4
(E) 5

Walking from K to O along the lines pick up the letters
KANGAROO in the correct order. What is the length of the shortest walk in meters?

(A) 16 m
(B) 17 m
(C) 18 m
(D) 19 m
(E) 20 m

## Homework Review

4 Daniel has a few boxes with pencils. In each box there are either 3 or 5 pencils.
All boxes are closed, he cannot open them and see how many pencils are inside the box. Answer each question by writing the expression to show how he can do it.
a) Can he get exactly 29 pencils without opening any boxes?
b) Can he get 14 pencils without opening any boxes?
c) Can he get 31 pencils without opening any boxes?

The table below shows how to add numbers from 1 to 9 .
Two squares are shaded blue and two are shaded green.

Q: Are the blue squares mirror images (diagonal colored yellow is a "mirror") of each other? Explain why?

Q: Are the green squares mirror images of each other? Explain why the numbers in the green squares are equal.

Find at least 5 more mirror image squares and shade those pairs with the same color. Why are the mirror image numbers always equal? What is the property of addition did you use?

| + | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 |
| 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 |
| 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 |
| 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 |
| 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
| 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 |
| 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 |

## New Material I

## Rotational Symmetry

A shape has Rotational Symmetry when it still looks the same after some rotation (of less than one full turn).
The order of rotational symmetry is the number of times an object or shape can be rotated and still look like it did before rotation began.

Think of propeller blades, it will be easier to see orders of rotational symmetry.


There also could be the Orders $5,6,7,9,10$ and so on $\ldots$

## Is there Rotational Symmetry of Order 1 ?

Not really! If a shape only matches itself once as we go around (i.e., it matches itself after one full rotation) there is really no symmetry at all ...
... because the word "Symmetry" comes from syn-together and metron measure, and there can't be "together" if there is just one thing.

What is the order of rotational symmetry for a star? $\qquad$
What is the order of rotational symmetry for a right triangle? $\qquad$



4

5


7 Examples: a) Road signs may possess rotational symmetry:


Order 4


Order 2


Order 3
Order1 (No rotational symmetry)
8. What is the order of rotational symmetry of the shapes below?

(3)

(2)

(4)


(6)

(7)


REVIEW I

9
a) Not every shape has a line of symmetry. Which of the four shapes below have a line of symmetry? Draw a line of symmetry on them.

b) Some shapes have many lines of symmetry. Draw all the lines of symmetry you can find on the shape below. How many are there?


11 Calculate:
$\qquad$ $7 \times 1=$ $\qquad$ $0 \times 4=$ $\qquad$
$1 \times 17=$ $\qquad$
$0 \times 18=$ $\qquad$ $1 \times 9=$ $\qquad$ $15 \times 1=$ $\qquad$
$100 \times 0=$ $\qquad$
$100 \times 1=$ $\qquad$
$15 \times 10=$ $\qquad$ $10 \times 27=$ $\qquad$

12 Circle all even numbers. How do you know that the number is even?
$1,4,140,254,327,806,548,914,789$

## REVIEW II

## Properties of Addition

| Commutative property | You can add in any order | $3+6=6+3=9$ |
| :--- | :--- | :--- |
| Associative property | You can group the numbers in any <br> combination | $2+(3+4)=(2+4)+3=9$ |

Remember the addition table of numbers from 1 to 3 ?
Why do the pairs of numbers in blue squares and orange squares are "mirror" images of each other?

| + | 1 | 2 | 3 |
| :---: | :---: | :---: | :---: |
| 1 | 2 | 3 | 4 |
| 2 | 3 | 4 | 5 |
| 3 | 4 | 5 | 6 |

The identity element is defined as the element (number) that, when used in a mathematical operation with another number, leaves that number unchanged.

In the case of addition, that element is the number 0 (zero).

| Identity property of addition | The sum of any number and zero <br> is the number | $9+0=9$ |
| :--- | :--- | :--- |

Calculate smartly, using the properties of addition:
$0+52=$ $\qquad$
$52-0=$
$50+2=$ $\qquad$ $24+(26+2)=$ $\qquad$
$a+0=$ $\qquad$
$\boldsymbol{a}-0=$ $\qquad$
$a+b=$ $\qquad$ $a+(b+c)=$ $\qquad$

## New Material II

## Properties of Multiplication

| Commutative property | You can multiply in any order | $3 \times 6=6 \times 3=18$ |
| :--- | :--- | :--- |
| Associative property | When you multiply you can <br> group the numbers in any <br> combination | $2 \times(3 \times 4)=(2 \times 4) \times 3=24$ |
| Identity property | The product of 1 and any <br> number is the number | $9 \times 1=9$ |

15 What is Identity element for multiplication? $\qquad$

16 Solve the equations:
$9 \times x=9$
$p \times 7=7$
$22 \times r=0$
$q \times 17=0$
$x=$ $\qquad$
p $=$ $\qquad$
$r=$ $\qquad$
$q=$ $\qquad$

17
Rewrite each problem using the associative property of multiplication and find the answer.

$$
\begin{aligned}
& (10 \times 5) \times 8= \\
& (7 \times 11) \times 2= \\
& 9 \times(2 \times 7)= \\
& \hline
\end{aligned}
$$

18 Which of the examples below illustrates the commutative property of multiplication and which associative property?
$6 \times 1=6$

$$
9 \times 3=3 \times 9
$$

$6 \times(2 \times 7)=(6 \times 2) \times 7$
$9 \times(3 \times 7)=(9 \times 3) \times 7$
$6 \times 2=2 \times 6$
$82 \times 18=18 \times 82$

