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Rotational Symmetry. Properties of multiplication.

Homework Review

Daniel has a few boxes with pencils. In each box there are either 3 or 5 pencils.

All boxes are closed, he cannot open them and see how many pencils are inside the box. Answer each question by writing the expression to show how he can do it. a) Can he get exactly 29 pencils without opening any boxes?

b) Can he get 14 pencils without opening any boxes?

c) Can he get 31 pencils without opening any boxes?

The table below shows how to add numbers from 1 to 9. Two squares are shaded blue and two are shaded green.

Q: Are the blue squares mirror images (diagonal colored yellow is a "mirror") of each other? Explain why?

Q: Are the green squares mirror images of each other? Explain why the numbers in the green squares are equal.

Find at least 5 more mirror image squares and shade those pairs with the same color. Why are the mirror image numbers always equal? What is the property of addition did you use?

+	1	2	3	4	5	6	7	8	9
1	2	3	4	5	6	7	8	9	10
2	3	4	5	6	7	8	9	10	11
3	4	5	6	7	8	9	10	11	12
4	5	6	7	8	9	10	11	12	13
5	6	7	8	9	10	11	12	13	14
6	7	8	9	10	11	12	13	14	15
7	8	9	10	11	12	13	14	15	16
8	9	10	11	12	<mark>13</mark>	14	15	16	17
9	10	11	12	13	14	15	16	17	18

Lesson 19

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New Material I

Rotational Symmetry

A shape has **Rotational Symmetry** when it still looks the same after some rotation (of less than one full turn).

The **order of rotational symmetry** is the number of times an object or shape can be rotated and still look like it did before rotation began.

Think of propeller blades, it will be easier to see orders of rotational symmetry.



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There also could be the Orders 5, 6, 7, 9, 10 and so on ...

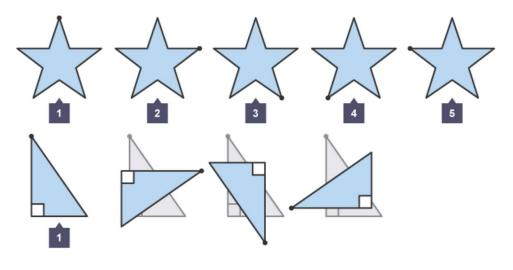
Is there Rotational Symmetry of Order 1?

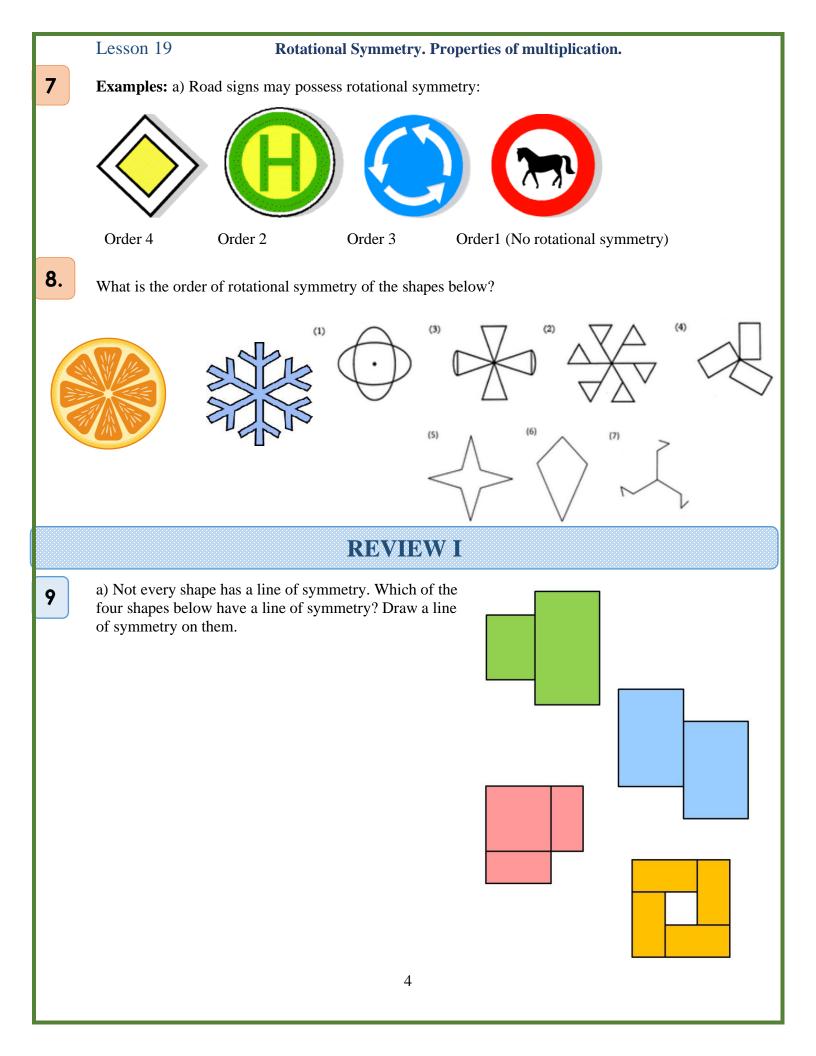
Not really! If a shape only matches itself **once** as we go around (i.e., it matches itself after one full rotation) there is really no symmetry at all ...

... because the word "Symmetry" comes from *syn-* together and *metron* measure, and there can't be "together" if there is just one thing.

What is the order of rotational symmetry for a star?

What is the order of rotational symmetry for a right triangle?





	Lesson 19Rotational Symmetry. Properties of multiplication.					
10	· · · ·	s of symmetry. Draw all the lines of nape below. How many are there?				
11						
		0 × 4 = 1				
		1 × 9 = 1				
	$100 \times 0 = _$ $100 \times 1 =$	$15 \times 10 = $ 10	$3 \times 27 = $			
12	12 Circle all even numbers. How do you know that the number is even? 1, 4, 140, 254, 327, 806, 548, 914, 789					
	REVIEW II					
Properties of Addition						
	Commutative propertyYou can add in any order $3+6=6+3=9$					
	Associative propertyYou can group the numbers in any combination $2 + (3 + 4) = (2 + 4) + 3 = 9$					
13	Remember the addition table of	numbers from 1 to 3?	+ 1 2 3			
	Why do the pairs of numbers in "mirror" images of each other?	blue squares and orange squares are	1 2 3 4			
			2 3 4 5			
			3 4 5 6			
The identity element is defined as the element (number) that, when used in a mathematical operation with another number, leaves that number unchanged. In the case of addition, that element is the number 0 (zero).						
	Identity property of addition	The sum of any number and zero is the number	9 + 0 = 9			
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Lesson 19

Rotational Symmetry. Properties of multiplication.

14 Calculate smartly, using the properties of addition:

$$0 + 52 = _ 52 - 0 = 50 + 2 = _ 24 + (26 + 2) = _ a + 0 = _ a + b = _ a + (b + c) = _ a + (b$$

New Material II

Properties of Multiplication

Commutative property	You can multiply in any order	$3 \times 6 = 6 \times 3 = 18$
Associative property	When you multiply you can group the numbers in any combination	$2 \times (3 \times 4) = (2 \times 4) \times 3 = 24$
Identity property	The product of 1 and any number is the number	9 × 1 = 9

15 What is Identity element for multiplication?

Solve the equations:			
$9 \times x = 9$	$\boldsymbol{p} imes 7 = 7$	$22 \times \mathbf{r} = 0$	$\boldsymbol{q} \times 17 = 0$
<i>x</i> =	<i>p</i> =	<i>r</i> =	<i>q</i> =
	Solve the equations: $9 \times x = 9$ x =	•	-

17 Rewrite each problem using the associative property of multiplication and find the answer.

 $(10 \times 5) \times 8 =$ _____ $(7 \times 11) \times 2 =$ _____ $9 \times (2 \times 7) =$ _____

18 Which of the examples below illustrates the commutative property of multiplication and which - associative property?

$6 \times 1 = 6$	$9 \times 3 = 3 \times 9$
$6 \times (2 \times 7) = (6 \times 2) \times 7$	$9 \times (3 \times 7) = (9 \times 3) \times 7$
$6 \times 2 = 2 \times 6$	$82 \times 18 = 18 \times 82$