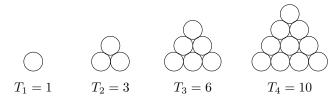
MATH 8: HANDOUT 7 MORE COMBINATORICS

These are some additional combinatorics problems.

- 1. How many ways there are to group 2n people into n pairs? [Pairs are not numbered.]
- **2.** How many different "words" can be formed by permuting letters of the word "letter"? of the word "Mississippi"? (by "word", we mean any sequence of letters, not necessarily meaningful").
- **3.** How many ways there are to arrange 12 books on 2 bookshelves (top and bottom one)? The order on each bookshelf matters; there are no restrictions on how many of the 12 books are on top shelf.
- **4.** How many different monomials in 3 variables x, y, z of total degree n are there? in 4 variables?
- **5.** Let T_n be the number of circles in a triangular shape with n levels like the ones below (these are sometimes called *triangular* numbers):



- (a) Note that $T_3 = T_2 + 3$, and $T_4 = T_3 + 4$. Is it true that in general, $T_n = T_{n-1} + n$? Why or why not?
- (b) Look at Pascal triangle. Can you find these numbers there?
- (c) Can you write a general formula for T_n ?
- *6. What if instead of drawing circles on plane, we were arranging balls in a pyramid? Can you guess how many balls we would have in pyramid with 1 level; with 2, 3, 4 levels? Can you find these numbers in Pascal triangle?