

Work and Kinetic Energy

2nd Newton's Law can be rewritten as:

$$m\Delta v = F\Delta t$$

$$mv\Delta v = F(v\Delta t)$$

One can show that the left-hand-side is a change in Kinetic energy, $K = \frac{mv^2}{2}$

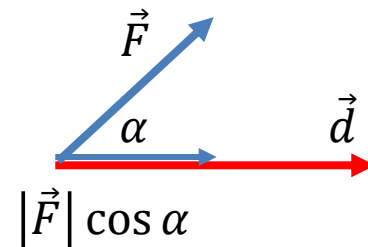
The right hand side (Force times Displacement) is called work, $W = F\Delta x$

This leads to a very important result:

$$\Delta K = W$$

A more general definition of work when Force and Displacement are given as vectors \vec{F} and \vec{d} (in 2D or 3D case):

$$W = |\vec{F}||\vec{d}| \cos \alpha$$



Homework

Problem 1.

The car moves at speed v when suddenly the driver applies breaks. Find the distance the car will travel before coming to a complete stop, if the friction coefficient is μ . Use the Kinetic Energy theorem ($\Delta K=W$) to solve this problem.

Problem 2

An object of mass $m=1kg$ is placed on a horizontal plane with coefficient of kinetic friction $\mu=0.5$. It is moved along the triangular trajectory $A \rightarrow B \rightarrow C \rightarrow A$ (see Figure), and returns to the initial point A. Find the work done *by friction*, if $AB=40\text{ cm}$ and $AC=30\text{ cm}$. Remember that friction force is directed opposite to the direction of motion.

