

# Momentum and Impulse

$$\vec{F} = ma = m \frac{\Delta \vec{v}}{\Delta t},$$

$$\Delta \vec{p} = \vec{F} \Delta t$$

$\vec{p} = m\vec{v}$  called Momentum

$\vec{F}\Delta t$  called Impulse

If  $\mathbf{F}$  changes with time, Impulse is time integral of Force:

$$\Delta \vec{p} = \int_{t_1}^{t_2} \vec{F} dt$$

# Conservation of Momentum

2<sup>nd</sup> Newton's Law  
for  $n$  objects:

$$\Delta \vec{p}_1 = \vec{F}_1 \Delta t$$

$$\Delta \vec{p}_2 = \vec{F}_2 \Delta t$$

.....

$$\Delta \vec{p}_n = \vec{F}_n \Delta t$$

3<sup>rd</sup> Newton's Law,  
no external forces!

$$\vec{F}_1 + \vec{F}_2 + \dots + \vec{F}_n = 0$$

$$\Delta(\vec{p}_1 + \vec{p}_2 + \dots + \vec{p}_n) = 0$$

$$\vec{p}_1 + \vec{p}_2 + \dots + \vec{p}_n = \text{const}$$

**Total Momentum of Isolated System is Conserved**

# Homework

## Problem 1

A tennis ball of mass  $m=57\text{ g}$  with initial velocity  $v=30\text{ m/s}$ , directed towards the wall bounces off it elastically. Using high-speed camera, it was determined that the collision time was about  $t=1\text{ ms}$  (1 millisecond). Estimate the maximum force between the wall and the ball.

## Problem 2

A block of mass  $M=100\text{ g}$  moves with speed of  $v=10\text{ m/s}$  on a frictionless flat surface. A bullet of mass  $m=8\text{ g}$  that moves with speed  $u=700\text{ m/s}$  in the opposite direction, hits the block and gets stuck in it. What will be the velocity of the block after this collision (include direction in your response)?