



5

What is the greatest number you can write in the box?

$\square + 8 < 12$

$11 - \square > 6$

$14 + \square < 20$

$100 > \square 9$

$\square 3 < 32$

$51 > 5 \square$

## New Material I

## Multiplication

*Question:* if we have 4 cars, and there are 3 persons in each car, how many people do we have altogether?

The answer can be obtained either by adding four times 3:  $3 + 3 + 3 + 3 = 12$

or by using operation of multiplication:

Instead of writing  $3 + 3 + 3 + 3$  (4 times), we write  $3 \times 4$

The simple multiplication can be understood intuitively as a repeated addition.

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Express the sum as a multiplication (do not calculate):

$2 + 2 = \underline{\hspace{2cm}}$

$3 + 3 = \underline{\hspace{2cm}}$

$100 + 100 = \underline{\hspace{2cm}}$

*Conclusion:* Multiplication by 2 doubles any numbers.

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Each group of coins contains 4 coins and there are 5 groups.



Altogether there are  $4 + 4 + 4 + 4 + 4 = 20$  coins  
5 times

Counting the same coins by multiplication yields:  $4 \times 5 = 20$

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Compare without calculating the values:

$2 + 2 + 2 + 2 \underline{\hspace{1cm}} 2 \times 5$

$3 \times 4 \underline{\hspace{1cm}} 4 + 4 + 4$

$3 \times 4 \underline{\hspace{1cm}} 3 + 3 + 3$

$3 \times 4 + 4 \underline{\hspace{1cm}} 4 + 4 + 4$

$5 \times 3 \underline{\hspace{1cm}} 5 + 5 \times 2$

$4 \times 5 \underline{\hspace{1cm}} 2 \times 5 + 2 \times 5$

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How many walnuts? Is the number of walnuts the same on both pictures?



### Objects in rectangular arrays:

If we have walnuts arranged in 3 rows and 4 columns, we can get the total number of walnuts in two ways:

a) *By rows:* (4 walnuts in each row)  $\times$  (3 rows) =  $4 \times 3 = 12$  walnuts

b) *By columns:* (3 walnuts in each column)  $\times$  (4 columns) =  $3 \times 4 = 12$  walnuts

The answer will be the same, no matter which way we use.

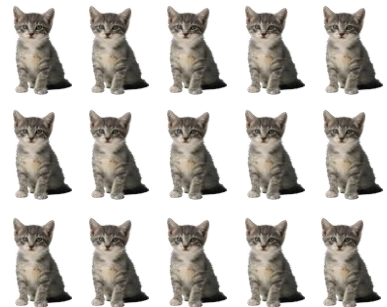
$$4 \times 3 = 3 \times 4 = 12$$

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Calculate the number of kittens using multiplication:

a) by row \_\_\_\_\_

b) by column: \_\_\_\_\_



Multiplying two whole numbers gives a **product**. The numbers that we multiply are **the factors of the product**.

*Example:*  $3 \times 4 = 12$  therefore, 3 and 4 are the factors of 12.

Also  $2 \times 6 = 12$ , so 2 and 6 are also factors of 12,

And  $1 \times 12 = 12$ , so 1 and 12 are factors of 12 as well.

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a) In each equation, underline the factors of the products and circle the products.

$1 \times 5 = 5$

$2 \times 5 = 10$

$1 \times 5 = 5$

$4 \times 5 = 20$

b) Express each multiplication as a repetitive sum.

*Example:*  $2 \times 5 = 5 + 5 = 2 + 2 + 2 + 2 + 2$

$1 \times 5 = \underline{\hspace{4cm}}$

$3 \times 5 = \underline{\hspace{4cm}}$

$2 \times 6 = \underline{\hspace{4cm}}$

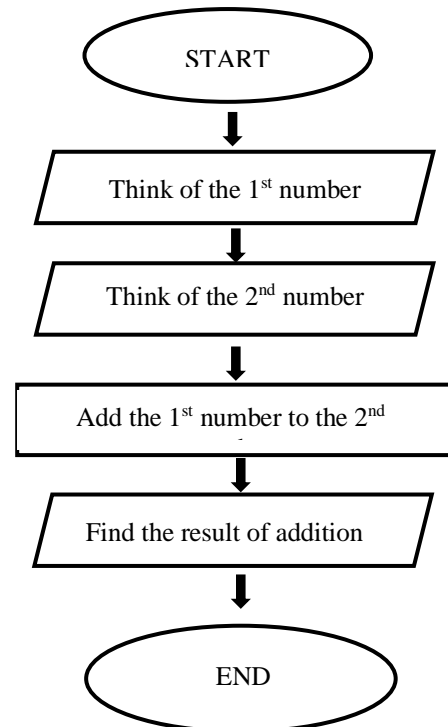
## REVIEW I

A **linear algorithm** is a step-by-step instruction, and the order of those instructions is essential.

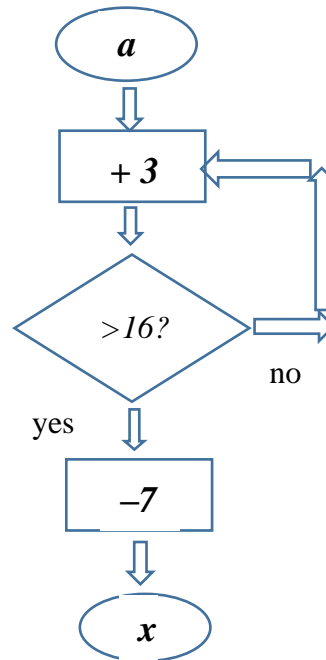
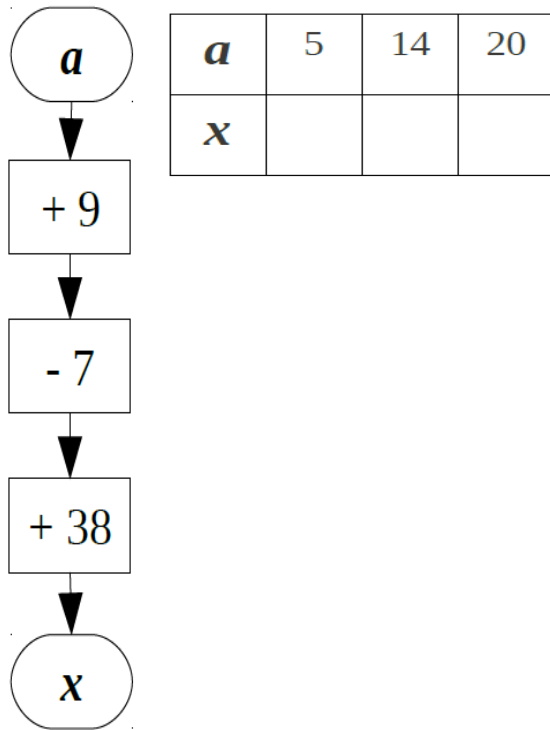
A **Cycling algorithm**: In some programs, certain steps are performed again and again based upon the conditional test, i.e., performed more than one time. Those steps are called a loop.

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Example of the Linear algorithm.



- 13** Perform the actions according to the algorithms in the drawing below. Which of these algorithms is linear and which one is cycling? Explain.



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## REVIEW II

- |                                    |  |
|------------------------------------|--|
| 1. Adding number to a sum          | $(33 + 74) + 26 = 33 + (74 + 26) = 33 + 100 = 133$   |
| 2. Subtracting number from a sum   | $(137 + 92) - 37 = (137 - 37) + 92 = 100 + 92 = 192$ |
| 3. Subtracting a sum from a number | $128 - (28 + 14) = (128 - 28) - 14 = 100 - 14 = 86$  |

- 14** Calculate smartly (the most convenient way):

$$75 - (34 + 25) =$$

$$91 - (71 + 15) =$$

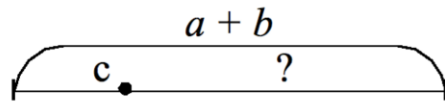
$$(29 + 36) - 19 =$$

$$(13 + 57) - 47 =$$

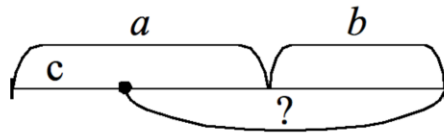
$$2 + (36 + 98) =$$

**15** There were  $a$  liters of water in the 1<sup>st</sup> bucket and  $b$  liters of water in the 2<sup>nd</sup> bucket. A gardener used  $c$  liters of water to water his garden. How many liters of water remained in both buckets total?

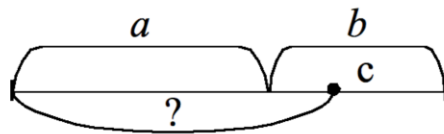
There are three different methods to solve this problem. Let's consider each of them.



Method I :  $(a + b) - c$



Method II :  $(a - c) + b$



Method III :  $a + (b - c)$

$$(a + b) - c = (a - c) + b = (b - c) + a = a + b - c$$

### Did you know ...

**Algorithms** have a long history. The word can be traced back to the 9th century.

At this time, the Persian scientist, astronomer, and mathematician Abdullah Muhammad bin Musa al-Khwarizmi, often cited as "The father of Algebra," was indirectly responsible for creating the term "Algorithm." In the 12th century, one of his books was translated into Latin, where his name was rendered in Latin as "Algorithm." But this was not the beginning of algorithms.

In 1600 BC - Babylonians develop the earliest known algorithms. The concept of the algorithm was formalized in 1936 through Alan Turing's Turing machines, which in turn formed the foundation of computer science.