

MATH 6: HANDOUT 0
REVIEW PROBLEMS

PROBLEMS

1. Rewrite each of the expressions below in the simplest possible form, by collecting the like terms if possible.

$$\begin{array}{lll} 2x + 7 + 5x + 2 + 3x & 3x + 9 + 5xy + 2xy + 3 & 3(2x - 1) + x \\ 2a(a - 2) - a(a - 1) & (2x - 1)(x + 1) & \end{array}$$

2. An apple cost 9 cents, and an orange 15 cents. Elena bought some apples and oranges, 20 fruit in all, and paid \$2.64. How many apples and how many oranges did she buy?
3. A boy had a bag of apples. He gave $\frac{1}{2}$ of them to his parents, $\frac{1}{5}$ to his brother, $\frac{1}{4}$ to his sister and the last apple he ate himself. How many apples did he originally have?
4. Simplify the following expressions
- (a) $x + 4(1 - x)$ (b) $2 + 5x - 4(3 - x)$ (c) $5(x - 1) - 3(2x + 1)$
5. If you take half my age and add 7, you get my age 13 years ago. How old am I?
6. Two secretaries, Barbara and Mary, need to type a 100 page document. Barbara can type it in 4 hours; Mary types slower, so it would take her 5 hours to do this. How fast can they type it together if they divide the work between two of them in the most efficient way?
7. Find the sum $1 + 2 + 4 + \dots + 2^n$ (the answer, of course, will depend on n). [Hint: first try computing it for several small values of n : find $1 + 2$, then $1 + 2 + 4$, then $1 + 2 + 4 + 8$. See if you can notice a pattern. After this, try formulating a general rule.]
8. Convert the decimal numbers to binary:
9, 12, 24, 38, 45
9. Convert the following binary numbers to decimal:
101, 1001, 10110, 11011, 10101
10. Compute $110101_b + 111011_b$ without converting numbers to decimal form.
11. Simplify the following expression:

$$\frac{(x^2y^2) \cdot x^3}{x^2y^5}$$

12. Let $a = 2 \cdot 10^8$, $b = 10^5$. Compute $a^2 \cdot b$, $\frac{a}{b}$, $a^2 \div b^3$.
13. If $a = 2^{-13}3^9$, $b = 2^{11}3^{-7}$, what is the value of ab ? of a/b ?
14. Write the following numbers using scientific notation.
- (a) the distance from Earth to Pluto is $\approx 7,527,000,000$ km;
- (b) the distance from Earth to the star Sirius is $\approx 81,900,000,000,000$ km;

15. Factor the following number into primes: $99^2 - 9^2$. [Hint: you do not have to compute this number.]
16. Find the following square roots. If you can not find the number exactly, at least say between which two whole numbers the answer is, e.g., between 5 and 6.
- (a) $\sqrt{81}$
 (b) $\sqrt{10,000}$
 (c) $\sqrt{10^8}$
17. If, in a right triangle, one leg has length 1 and the hypotenuse has length 2, what is the other leg?
18. Simplify: $(\sqrt{17})^2$, $(\sqrt{13})^4$, $(\sqrt{11})^3$, $\sqrt{2^4 3^6}$, $\sqrt{2^4 3^5}$.
19. We roll two dice. What is the probability of getting sum of two numbers equal to 4?
20. If we toss a coin 5 times, what is the probability that **at least one** will be heads?
21. A license plate consists of 3 letters, followed by three digits. How many possible license plates are there?
22. We roll two identical dice. What is the probability of getting 1 and 3?
23. We roll two identical dice. What is the probability of getting sum of two numbers equal to 4?
24. If we toss a coin 5 times, what is the probability that at least one will be heads?
25. How many ways are there to seat 15 students in a classroom which has 15 chairs?
 If the room has 25 chairs?
26. Solve equations:
- (a) $\frac{3}{8}x = \frac{1}{3}$ (b) $|2x - 5| = 1$ (c) $\frac{x - 2}{x - 1} = 3$