

Momentum and Impulse

$$\vec{F} = ma = m \frac{\Delta \vec{v}}{\Delta t},$$

$$\Delta \vec{p} = \vec{F} \Delta t$$

$\vec{p} = m\vec{v}$ called Momentum

$\vec{F}\Delta t$ called Impulse

Conservation of Momentum

2nd Newton's Law
for n objects:

$$\Delta \vec{p}_1 = \vec{F}_1 \Delta t$$

$$\Delta \vec{p}_2 = \vec{F}_2 \Delta t$$

.....

$$\Delta \vec{p}_n = \vec{F}_n \Delta t$$

3rd Newton's Law,
no external forces!

$$\vec{F}_1 + \vec{F}_2 + \dots + \vec{F}_n = 0$$

$$\Delta(\vec{p}_1 + \vec{p}_2 + \dots + \vec{p}_n) = 0$$

$$\vec{p}_1 + \vec{p}_2 + \dots + \vec{p}_n = \text{const}$$

Total Momentum of Isolated System is Conserved

Homework

Problem 1

A block of mass $M=100\text{g}$ moves with speed of $v=10\text{m/s}$ on a frictionless flat surface. A bullet of mass $m=8\text{g}$ that moves with speed $u=700\text{ m/s}$ in the opposite direction, hits the block and gets stuck in it. What will be the velocity of the block after this collision (include direction in your response)?

Problem 2

An empty bottle rocket has mass $M=100\text{ g}$. It is filled with $m=800\text{g}$ of water. During the launch, the water quickly jets out of the nozzle with average speed $v=5\text{m/s}$ (in the reference frame of the ground). Find the speed of the rocket after it empties.