

Warm Up

1

Multiplication and Division Quiz. Do as many problems as you can in **3 minutes**.



$5 \times 0 =$

$3 \times 15 =$

$60 \times 5 =$

$10 \times 5 =$

$4 \times 3 =$

$40 \times 4 =$

$6 \times 3 =$

$6 \times 2 =$

$6 \times 4 =$

$8 \times 1 =$

$8 \times 10 =$

$8 \times 50 =$

$2 \times 7 =$

$20 \times 9 =$

$2 \times 6 =$

$9 \times 100 =$

$9 \times 5 =$

$9 \times 3 =$

$7 \times 6 =$

$8 \times 7 =$

$7 \times 7 =$

$10 \div 2 =$

$20 \div 4 =$

$20 \div 5 =$

$16 \div 8 =$

$16 \div 2 =$

$30 \div 15 =$

$30 \div 6 =$

$35 \div 5 =$

$30 \div 10 =$

2

To get one glass of freshly squeezed orange juice, we need to take 4 oranges. How many oranges do we need to take to make 10L of orange juice? (1L is 4 full glasses)

Homework Review

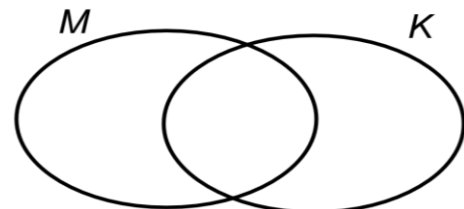
3

Consider sets **M** and **K**. By using { }, define the elements of the set **M ∩ K**. Mark the elements of the sets **M** and **K** on the Venn diagram and trace with a colored pencil the set **M ∩ K**.

a) _____

$M = \{ 15, 25, 30, 40 \}$

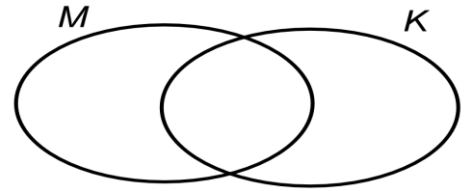
$K = \{ 23, 24, 25 \}$



b) _____

$$M = \{ \star, \square, a, b \}$$

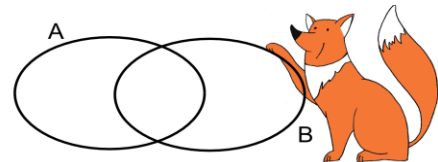
$$K = \{ \square, a, d \}$$



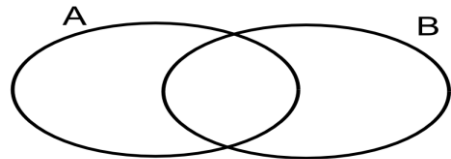
4

Place 4 elements $\{x, y, z, q\}$ on the diagrams of the sets A and B so that there would be:

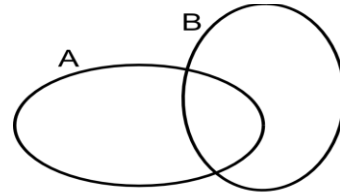
a) 3 elements in each set;



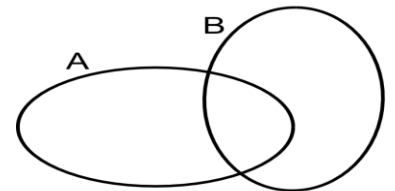
b) 2 elements in one set and 4 elements in the other;



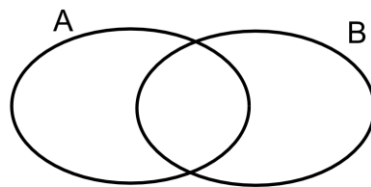
c) 4 elements in one set and 3 elements in the other;



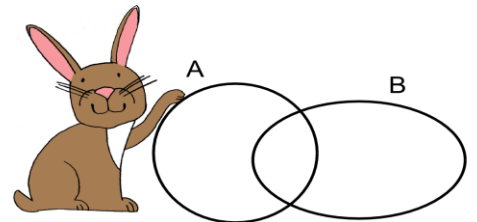
d) 0 elements in one set and 4 elements in the other;



e) 4 elements in each set;



f) 2 elements in each set.



New Material II

Two sets are called **equal** if they have exactly the same elements. Thus, following the usual convention that 'y' is not a vowel, the set $C = \{\text{vowels in the English alphabet}\} = \{a, e, i, o, u\}$

On the other hand, the sets $A = \{1, 3, 5\}$ and $B = \{1, 2, 3\}$ are not equal, because they have different elements. This is written as $\{1, 3, 5\} \neq \{1, 2, 3\}$ or $A \neq B$

The order in which the elements are written between the curly brackets does not matter at all. For example,

$$\{1, 3, 5, 7, 9\} = \{3, 9, 7, 5, 1\} = \{5, 9, 1, 3, 7\}.$$

If an element is listed more than once, it is only counted once. For example, $\{a, a, b\} = \{a, b\}$.

The set $\{a, a, b\}$ has only the two elements a and b . The second mention of a is an unnecessary repetition and can be ignored. It is normally considered poor notation to list an element more than once.

9

a) Set C is a set of all multiples of number 15. The set D is a set of all multiples of a number 18. Are sets C and D equal? Explain. _____

b) Set E is a set of all multiples of number 36. The set F is a set of all multiples of a number 12. Are sets E and F equal? Explain. _____

The phrases 'is an element of' and 'is not an element of' occur so often in discussing sets that the special symbols \in and \notin are used for them. For example, if $A = \{3, 4, 5, 6\}$, then

$3 \in A$ (Read this as '3 is an element of the set A '.)

$8 \notin A$ (Read this as '8 is not an element of the set A '.)

10

a) The set A is the set of all even numbers.

Does 100 belong to the set A ?

Does 1001 belong to the set A ?

b) The set B is the set of all numbers divisible by 4.

Does 88 belong to the set B ?

Does 100 belong to the set B ?

Did you know ...

The benefits of analyzing math problems before starting to solve them.

There was a boy in a class studying math with, of course, a math teacher. This boy's name is Carl Friedrich Gauss (1777 - 1855). One day this math teacher presented a challenging mathematical problem to the class where Gauss is in.

The math problem is to add up all the numbers starting from 1 and ending with 100. Every students picked up a piece of paper and started to add up the numbers one after another from number 1 onwards.

Within a short span of time, while his fellow students were still struggling, Gauss went forward to the teacher and submitted his answer.

That action surprised not only his math teacher but the whole class. But that is not all... The interesting thing is that his answer is correct.

How did he do that so fast?

He came out a different way of analyzing the mathematical problem. Instead of the normal way of adding the first numbers onwards, Gauss looked at the problem with a different angle.

What he did was to split the range of number from 1 to 100 into two equal halves, 1 to 50 and 51 to 100. He noticed that if he flipped the last half to start from 100, and adding it the two ranges together, he will get something stunning.

He discovered that by adding the first pair, $1 + 100$, he got an answer of 101. For the second pair, $2 + 99$, he again got the same answer 101.

This answer of 101 was still valid for the rest of the number pair addition. And since there were 50 pairs of numbers, the final total is 101×50 which gave Gauss an answer of 5050.